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# **dnn-inference**

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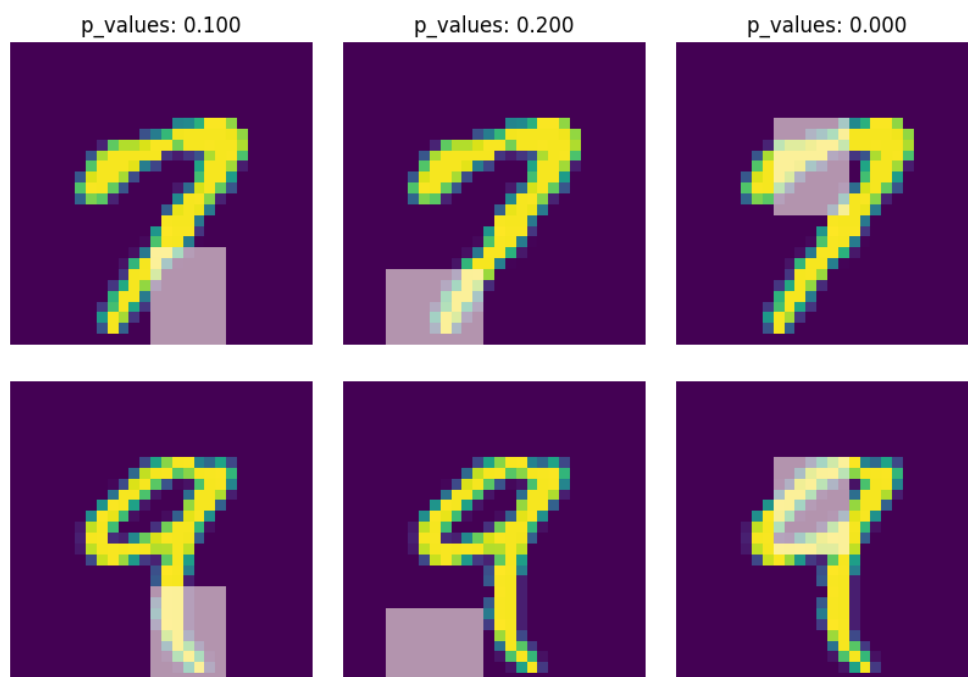


**dnn-inference** is a Python module for hypothesis testing based on blackbox models, including **deep neural networks**.

- GitHub repo: <https://github.com/statmlben/dnn-inference>
- Documentation: <https://dnn-inference.readthedocs.io>
- PyPi: <https://pypi.org/project/dnn-inference>
- Open Source: MIT license
- Paper: [arXiv:2103.04985](https://arxiv.org/abs/2103.04985)



## WHAT WE CAN DO



**dnn-inference** is able to provide an asymptotically valid *p-value* to examine if  $\mathcal{S}$  is discriminative features to predict  $Y$ . Specifically, the proposed testing is:

$$H_0 : R(f^*) - R_{\mathcal{S}}(g^*) = 0, \quad \text{versus} \quad H_a : R(f^*) - R_{\mathcal{S}}(g^*) < 0,$$

where  $\mathcal{S}$  is a collection of hypothesized features,  $R$  and  $R_{\mathcal{S}}$  are risk functions with/without the hypothesized features  $\mathbf{X}_{\mathcal{S}}$ , and  $f^*$  and  $g^*$  are population minimizers on  $R$  and  $R_{\mathcal{S}}$  respectively. The proposed test just considers the difference between the best predictive scores with/without hypothesized features. Please check more details in our paper [arXiv:2103.04985](https://arxiv.org/abs/2103.04985).

- When *log-likelihood* is used as a loss function, then the test is equivalent to a conditional independence test:  $Y \perp X_{\mathcal{S}} | X_{\mathcal{S}^c}$ .
- Only a *small number of fitting* on neural networks is required, and the number can be as small as 1.
- Asymptotically Type I error control and power consistency.





## REFERENCE

If you use this code please star the repository and cite the following paper:

```
@misc{dai2021significance,  
  title={Significance tests of feature relevance for a blackbox learner},  
  author={Ben Dai and Xiaotong Shen and Wei Pan},  
  year={2021},  
  eprint={2103.04985},  
  archivePrefix={arXiv},  
  primaryClass={stat.ML}  
}
```



## CONTENTS

### 3.1 Installation

#### 3.1.1 Dependencies

dnn-inference requires: **Python**>=3.8 + [pip libs](./requirements.txt)

```
pip install -r requirements.txt
```

#### 3.1.2 User installation

Install dnn-inference using pip

```
pip install dnn_inference  
pip install git+https://github.com/statmlben/dnn-inference.git
```

#### 3.1.3 Source code

You can check the latest sources with the command.

```
git clone https://github.com/statmlben/dnn-inference.git
```

### 3.2 Examples

#### Contents

- *Examples*
  - *MNIST dataset*
  - *Boston Housing Dataset*

### 3.2.1 MNIST dataset

.sig\_test.split\_test in MNIST dataset

```
[2]: import numpy as np
      from tensorflow import keras
      from tensorflow.keras.datasets import mnist
      from tensorflow.keras.models import Sequential
      from tensorflow.keras.layers import Dense, Dropout, Flatten, Conv2D, MaxPooling2D
      from tensorflow.python.keras import backend as K
      import time
      from sklearn.model_selection import train_test_split
      from tensorflow.keras.optimizers import Adam, SGD
```

```
[4]: np.random.seed(0)
      num_classes = 2
      # input image dimensions
      img_rows, img_cols = 28, 28

      # the data, split between train and test sets
      (x_train, y_train), (x_test, y_test) = mnist.load_data()
      X = np.vstack((x_train, x_test))
      y = np.hstack((y_train, y_test))
      ind = (y == 9) + (y == 7)
      X, y = X[ind], y[ind]
      X = X.astype('float32')
      X += .01*abs(np.random.randn(14251, 28, 28))
      y[y==7], y[y==9] = 0, 1

      if K.image_data_format() == 'channels_first':
          X = X.reshape(x.shape[0], 1, img_rows, img_cols)
          input_shape = (1, img_rows, img_cols)
      else:
          X = X.reshape(X.shape[0], img_rows, img_cols, 1)
          input_shape = (img_rows, img_cols, 1)

      X /= 255.

      # convert class vectors to binary class matrices
      y = keras.utils.to_categorical(y, num_classes)
```

```
[5]: ## define the learning models
      def cnn():
          model = Sequential()
          model.add(Conv2D(32, kernel_size=(3, 3), activation='relu', input_shape=input_shape))
          model.add(Conv2D(64, (3, 3), activation='relu'))
          model.add(MaxPooling2D(pool_size=(2, 2)))
          model.add(Dropout(0.25))
          model.add(Flatten())
          model.add(Dense(128, activation='relu'))
          model.add(Dropout(0.5))
          model.add(Dense(num_classes, activation='softmax'))
```

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```

    model.compile(loss=keras.losses.binary_crossentropy, optimizer=keras.optimizers.
→Adam(0.0005), metrics=['accuracy'])
    return model

model_null, model_alter = cnn(), cnn()

2022-06-29 16:58:55.239237: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-06-29 16:58:55.243474: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-06-29 16:58:55.243767: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-06-29 16:58:55.244460: I tensorflow/core/platform/cpu_feature_guard.cc:151] This
→TensorFlow binary is optimized with oneAPI Deep Neural Network Library (oneDNN) to use
→the following CPU instructions in performance-critical operations: AVX2 AVX512F FMA
To enable them in other operations, rebuild TensorFlow with the appropriate compiler
→flags.
2022-06-29 16:58:55.245170: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-06-29 16:58:55.245475: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-06-29 16:58:55.245750: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-06-29 16:58:55.623115: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-06-29 16:58:55.623425: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-06-29 16:58:55.623674: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
→successful NUMA node read from SysFS had negative value (-1), but there must be at
→least one NUMA node, so returning NUMA node zero
2022-06-29 16:58:55.623925: I tensorflow/core/common_runtime/gpu/gpu_device.cc:1525]
→Created device /job:localhost/replica:0/task:0/device:GPU:0 with 3763 MB memory: ->
→device: 0, name: NVIDIA GeForce RTX 2060, pci bus id: 0000:01:00.0, compute capability:
→ 7.5

```

```

[6]: ## fitting param
from tensorflow.keras.callbacks import EarlyStopping
es = EarlyStopping(monitor='val_accuracy', mode='max', verbose=0, patience=15, restore_
→best_weights=True)

fit_params = {'callbacks': [es],
              'epochs': 50,
              'batch_size': 32,
              'validation_split': .2,

```

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```

        'verbose': 0}

## testing params
test_params = { 'split': "one-split",
                 'inf_ratio': None,
                 'perturb': None,
                 'cv_num': 2,
                 'cp': 'hommel',
                 'verbose': 2}

## tuning params
tune_params = { 'num_perm': 100,
                 'ratio_grid': [.2, .4, .6, .8],
                 'if_reverse': 0,
                 'perturb_range': 2.*np.arange(-3,3,.1),
                 'tune_ratio_method': 'fuse',
                 'tune_pb_method': 'fuse',
                 'cv_num': 2,
                 'cp': 'hommel',
                 'verbose': 2}

```

```

[7]: ## Inference based on dnn_inference
from sig_test import split_test
## testing based on learning models
inf_feats = [[np.arange(19,28), np.arange(13,20)], [np.arange(21,28), np.arange(4, 13)],
             ↪ [np.arange(7,16), np.arange(9,16)]]
cue = split_test(inf_feats=inf_feats, model_null=model_null, model_alter=model_alter, ↪
             ↪eva_metric='zero-one')
P_value = cue.testing(X, y, fit_params, test_params, tune_params)

INFO:tensorflow:Assets written to: ./saved/split_test/06-29_16-59/model_null_init/assets
2022-06-29 16:59:00.569380: W tensorflow/python/util/util.cc:368] Sets are not currently ↪
             ↪considered sequences, but this may change in the future, so consider avoiding using ↪
             ↪them.

INFO:tensorflow:Assets written to: ./saved/split_test/06-29_16-59/model_alter_init/assets
===== one-split for 0-th Hypothesis =====
2022-06-29 16:59:02.617064: I tensorflow/stream_executor/cuda/cuda_dnn.cc:368] Loaded ↪
             ↪cuDNN version 8101

(tuneHP: ratio) Est. Type 1 error: 0.000; inf sample ratio: 0.200
(tuneHP: ratio) Done with inf sample ratio: 0.200
(tuneHP: pb) Est. Type 1 error: 0.020; perturbation level: 0.125
(tuneHP: pb) Done with inf pb level: 0.125
cv: 0; p_value: 0.26510; loss_null: 0.00140(0.03744); loss_alter: 0.00175(0.04185)
cv: 1; p_value: 0.68497; loss_null: 0.00211(0.04583); loss_alter: 0.00175(0.04185)
0-th Hypothesis: accept H0 with p_value: 0.795
===== one-split for 1-th Hypothesis =====
(tuneHP: ratio) Est. Type 1 error: 0.000; inf sample ratio: 0.200
(tuneHP: ratio) Done with inf sample ratio: 0.200
(tuneHP: pb) Est. Type 1 error: 0.000; perturbation level: 0.125
(tuneHP: pb) Done with inf pb level: 0.125

```

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```

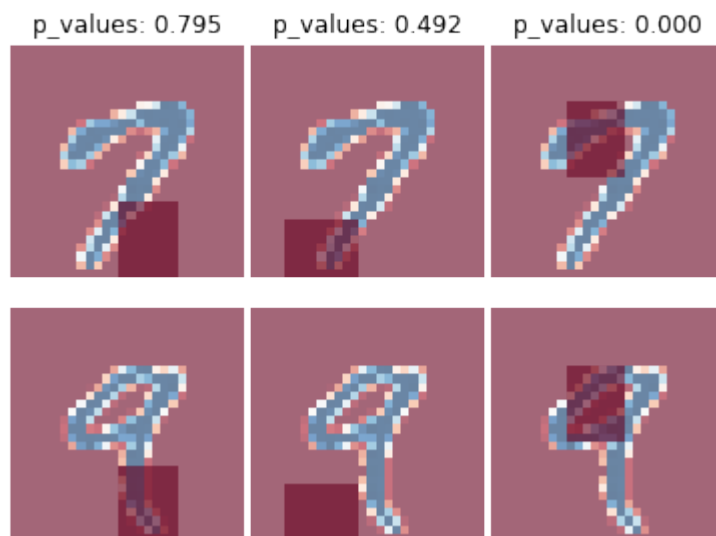
cv: 0; p_value: 0.16398; loss_null: 0.00140(0.03744); loss_alter: 0.00211(0.04583)
cv: 1; p_value: 0.92602; loss_null: 0.00316(0.05611); loss_alter: 0.00175(0.04185)
  1-th Hypothesis: accept H0 with p_value: 0.492
===== one-split for 2-th Hypothesis =====
(tuneHP: ratio) Est. Type 1 error: 0.020; inf sample ratio: 0.200
(tuneHP: ratio) Done with inf sample ratio: 0.200
(tuneHP: pb) Est. Type 1 error: 0.100; perturbation level: 0.125
(tuneHP: pb) Est. Type 1 error: 0.110; perturbation level: 0.134
(tuneHP: pb) Est. Type 1 error: 0.130; perturbation level: 0.144
(tuneHP: pb) Est. Type 1 error: 0.100; perturbation level: 0.154
(tuneHP: pb) Est. Type 1 error: 0.090; perturbation level: 0.165
(tuneHP: pb) Est. Type 1 error: 0.120; perturbation level: 0.177
(tuneHP: pb) Est. Type 1 error: 0.120; perturbation level: 0.189
(tuneHP: pb) Est. Type 1 error: 0.120; perturbation level: 0.203
(tuneHP: pb) Est. Type 1 error: 0.110; perturbation level: 0.218
(tuneHP: pb) Est. Type 1 error: 0.110; perturbation level: 0.233
(tuneHP: pb) Est. Type 1 error: 0.150; perturbation level: 0.250
(tuneHP: pb) Est. Type 1 error: 0.130; perturbation level: 0.268
(tuneHP: pb) Est. Type 1 error: 0.100; perturbation level: 0.287
(tuneHP: pb) Est. Type 1 error: 0.120; perturbation level: 0.308
(tuneHP: pb) Est. Type 1 error: 0.090; perturbation level: 0.330
(tuneHP: pb) Est. Type 1 error: 0.060; perturbation level: 0.354
(tuneHP: pb) Est. Type 1 error: 0.070; perturbation level: 0.379
(tuneHP: pb) Est. Type 1 error: 0.040; perturbation level: 0.406
(tuneHP: pb) Done with inf pb level: 0.406
cv: 0; p_value: 0.00000; loss_null: 0.00246(0.04950); loss_alter: 0.03088(0.17298)
cv: 1; p_value: 0.00000; loss_null: 0.00175(0.04185); loss_alter: 0.03298(0.17859)
  2-th Hypothesis: reject H0 with p_value: 0.000

```

```

[8]: ## visualize testing results
cue.visual(X,y)
print('P-values: %s' %P_value)

```



P-values: [0.7953140193691346, 0.49192858264606976, 1.1876805112986783e-19]

### 3.2.2 Boston Housing Dataset

.sig\_test.split\_test in Boston Housing price regression dataset

```
[1]: import numpy as np
import tensorflow.keras as keras
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Dense, Dropout, Flatten, Conv2D, MaxPooling2D
from tensorflow.python.keras import backend as K
import time
from sklearn.model_selection import train_test_split
from tensorflow.keras.optimizers import Adam, SGD
from sig_test import split_test
import tensorflow as tf
```

Boston house prices dataset

#### Data Set Characteristics:

Number of Instances: 506

Number of Attributes: 13 numeric/categorical predictive. Median Value (attribute 14) is usually the target.

#### Attribute Information (in order)

- CRIM per capita crime rate by town
- ZN proportion of residential land zoned for lots over 25,000 sq.ft.
- INDUS proportion of non-retail business acres per town
- CHAS Charles River dummy variable (= 1 if tract bounds river; 0 otherwise)
- NOX nitric oxides concentration (parts per 10 million)
- RM average number of rooms per dwelling
- AGE proportion of owner-occupied units built prior to 1940
- DIS weighted distances to five Boston employment centres
- RAD index of accessibility to radial highways
- TAX full-value property-tax rate per USD10,000
- PTRATIO pupil-teacher ratio by town
- B  $1000(B_k - 0.63)^2$  where  $B_k$  is the proportion of blacks by town
- LSTAT % lower status of the population
- MEDV Median value of owner-occupied homes in \$1000's

```
[2]: (x_train, y_train), (_, _) = tf.keras.datasets.boston_housing.load_data(path="boston_
    ↪housing.npz",
                                                    test_
    ↪split=0.1)
y_train, y_test = y_train[:, np.newaxis], y_test[:, np.newaxis]

from sklearn import preprocessing
scaler = preprocessing.MinMaxScaler()
x_train = scaler.fit_transform(x_train)
```



```
[3]: n, d = x_train.shape
      print('num of samples: %d, dim: %d' %(n, d))
```

num of samples: 455, dim: 13

```
[4]: from tensorflow import keras
      from tensorflow.keras import layers

      def build_model():
          model = keras.Sequential([
              layers.Dense(8, activation='relu', input_shape=[d]),
              layers.BatchNormalization(),
              layers.Dense(1, activation='relu')
          ])

          optimizer = tf.keras.optimizers.Adam(1e-3)

          model.compile(loss='mse',
                        optimizer=optimizer,
                        metrics=['mae', 'mse'])
          return model
```

```
[5]: model_null, model_alter = build_model(), build_model()
```

```
2022-06-30 12:53:52.290176: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
↳successful NUMA node read from SysFS had negative value (-1), but there must be at
↳least one NUMA node, so returning NUMA node zero
2022-06-30 12:53:52.295414: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
↳successful NUMA node read from SysFS had negative value (-1), but there must be at
↳least one NUMA node, so returning NUMA node zero
2022-06-30 12:53:52.295682: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
↳successful NUMA node read from SysFS had negative value (-1), but there must be at
↳least one NUMA node, so returning NUMA node zero
2022-06-30 12:53:52.296167: I tensorflow/core/platform/cpu_feature_guard.cc:151] This
↳TensorFlow binary is optimized with oneAPI Deep Neural Network Library (oneDNN) to use
↳the following CPU instructions in performance-critical operations: AVX2 AVX512F FMA
To enable them in other operations, rebuild TensorFlow with the appropriate compiler
↳flags.
2022-06-30 12:53:52.296992: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
↳successful NUMA node read from SysFS had negative value (-1), but there must be at
↳least one NUMA node, so returning NUMA node zero
2022-06-30 12:53:52.297257: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
↳successful NUMA node read from SysFS had negative value (-1), but there must be at
↳least one NUMA node, so returning NUMA node zero
2022-06-30 12:53:52.297500: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
↳successful NUMA node read from SysFS had negative value (-1), but there must be at
↳least one NUMA node, so returning NUMA node zero
2022-06-30 12:53:52.641227: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
↳successful NUMA node read from SysFS had negative value (-1), but there must be at
↳least one NUMA node, so returning NUMA node zero
2022-06-30 12:53:52.641520: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
↳successful NUMA node read from SysFS had negative value (-1), but there must be at
↳least one NUMA node, so returning NUMA node zero
```

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```

2022-06-30 12:53:52.641753: I tensorflow/stream_executor/cuda/cuda_gpu_executor.cc:936]
↳successful NUMA node read from SysFS had negative value (-1), but there must be at
↳least one NUMA node, so returning NUMA node zero
2022-06-30 12:53:52.642007: I tensorflow/core/common_runtime/gpu/gpu_device.cc:1525]
↳Created device /job:localhost/replica:0/task:0/device:GPU:0 with 3022 MB memory:  ->
↳device: 0, name: NVIDIA GeForce RTX 2060, pci bus id: 0000:01:00.0, compute capability:
↳ 7.5

```

```

[6]: from tensorflow.keras.callbacks import EarlyStopping
es = EarlyStopping(monitor='val_loss', mode='min',
                   verbose=0, patience=300, restore_best_weights=True)

fit_params = {'callbacks': [es],
              'epochs': 3000,
              'batch_size': 32,
              'validation_split': .2,
              'verbose': 0}

## testing params
test_params = { 'split': "one-split",
                'inf_ratio': None,
                'perturb': None,
                'cv_num': 2,
                'cp': 'hommel',
                'verbose': 2}

## tuning params
tune_params = { 'num_perm': 100,
                'ratio_grid': [.2, .4, .6, .8],
                'if_reverse': 1,
                'perturb_range': 2.**np.arange(-3,3,.3),
                'tune_ratio_method': 'fuse',
                'tune_pb_method': 'fuse',
                'cv_num': 2,
                'cp': 'hommel',
                'verbose': 2}

```

```

[7]: inf_feats = [np.arange(3), np.arange(5,11)]

cue = split_test(inf_feats=inf_feats, model_null=model_null, model_alter=model_alter,
↳eva_metric='mse')

P_value = cue.testing(x_train, y_train, fit_params, test_params, tune_params)

INFO:tensorflow:Assets written to: ./saved/split_test/06-30_12-53/model_null_init/assets
2022-06-30 12:53:59.491087: W tensorflow/python/util/util.cc:368] Sets are not currently
↳considered sequences, but this may change in the future, so consider avoiding using
↳them.

INFO:tensorflow:Assets written to: ./saved/split_test/06-30_12-53/model_alter_init/assets
===== one-split test for 0-th Hypothesis =====

```

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```

(tuneHP: ratio) Est. Type 1 error: 0.150; inf sample ratio: 0.800
(tuneHP: ratio) Est. Type 1 error: 0.270; inf sample ratio: 0.600
(tuneHP: ratio) Est. Type 1 error: 0.000; inf sample ratio: 0.400
(tuneHP: ratio) Done with inf sample ratio: 0.400
(tuneHP: pb) Est. Type 1 error: 0.000; perturbation level: 0.125
(tuneHP: pb) Done with inf pb level: 0.125
cv: 0; p_value: 0.03247; loss_null: 14.63722(51.76234); loss_alter: 18.41512(42.01610)
cv: 1; p_value: 0.01776; loss_null: 14.65350(46.57168); loss_alter: 21.16354(51.60448)
0-th Hypothesis: reject H0 with p_value: 0.049
===== one-split test for 1-th Hypothesis =====
(tuneHP: ratio) Est. Type 1 error: 1.000; inf sample ratio: 0.800
(tuneHP: ratio) Est. Type 1 error: 0.000; inf sample ratio: 0.600
(tuneHP: ratio) Done with inf sample ratio: 0.600
(tuneHP: pb) Est. Type 1 error: 0.700; perturbation level: 0.125
(tuneHP: pb) Est. Type 1 error: 0.730; perturbation level: 0.154
(tuneHP: pb) Est. Type 1 error: 0.700; perturbation level: 0.189
(tuneHP: pb) Est. Type 1 error: 0.700; perturbation level: 0.233
(tuneHP: pb) Est. Type 1 error: 0.610; perturbation level: 0.287
(tuneHP: pb) Est. Type 1 error: 0.580; perturbation level: 0.354
(tuneHP: pb) Est. Type 1 error: 0.470; perturbation level: 0.435
(tuneHP: pb) Est. Type 1 error: 0.460; perturbation level: 0.536
(tuneHP: pb) Est. Type 1 error: 0.390; perturbation level: 0.660
(tuneHP: pb) Est. Type 1 error: 0.290; perturbation level: 0.812
(tuneHP: pb) Est. Type 1 error: 0.180; perturbation level: 1.000
(tuneHP: pb) Est. Type 1 error: 0.190; perturbation level: 1.231
(tuneHP: pb) Est. Type 1 error: 0.170; perturbation level: 1.516
(tuneHP: pb) Est. Type 1 error: 0.070; perturbation level: 1.866
(tuneHP: pb) Est. Type 1 error: 0.070; perturbation level: 2.297
(tuneHP: pb) Est. Type 1 error: 0.030; perturbation level: 2.828
(tuneHP: pb) Done with inf pb level: 2.828
cv: 0; p_value: 0.12088; loss_null: 31.87867(120.14606); loss_alter: 34.30483(86.49743)
cv: 1; p_value: 0.83584; loss_null: 33.45124(124.96815); loss_alter: 33.72868(86.60861)
1-th Hypothesis: accept H0 with p_value: 0.363

```

[9]: P\_value

[9]: [0.048711537430423474, 0.3626513098329711]

### 3.3 API Reference

#### Contents

- *API Reference*
  - *dnn\_inference.sig\_test*
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### **3.3.1 dnn\_inference.sig\_test**

**dnn\_inference.sig\_test.split\_test**

**dnn\_inference.sig\_test.perm\_test**

**dnn\_inference.sig\_test.Hperm\_test**

## INDICES AND TABLES

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